

10. $y = \frac{1 - \sec x}{\tan x} \Rightarrow$

$$y' = \frac{\tan x (-\sec x \tan x) - (1 - \sec x)(\sec^2 x)}{(\tan x)^2} = \frac{\sec x (-\tan^2 x - \sec x + \sec^2 x)}{\tan^2 x} = \frac{\sec x (1 - \sec x)}{\tan^2 x}$$

12. $y = \csc \theta (\theta + \cot \theta) \Rightarrow$

$$y' = \csc \theta (1 - \csc^2 \theta) + (\theta + \cot \theta)(-\csc \theta \cot \theta) = \csc \theta (1 - \csc^2 \theta - \theta \cot \theta - \cot^2 \theta)$$

$$= \csc \theta (-\cot^2 \theta - \theta \cot \theta - \cot^2 \theta) \quad [1 + \cot^2 \theta = \csc^2 \theta]$$

$$= \csc \theta (-\theta \cot \theta - 2 \cot^2 \theta) = -\csc \theta \cot \theta (\theta + 2 \cot \theta)$$

29. $f(x) = x - 2 \sin x, 0 \leq x \leq 2\pi. f'(x) = 1 - 2 \cos x. \text{ So } f'(x) > 0 \Leftrightarrow 1 - 2 \cos x > 0 \Leftrightarrow -2 \cos x > -1 \Leftrightarrow \cos x < \frac{1}{2} \Leftrightarrow \frac{\pi}{3} < x < \frac{5\pi}{3} \Rightarrow f \text{ is increasing on } \left(\frac{\pi}{3}, \frac{5\pi}{3}\right).$

30. $f(x) = x - \sin x, 0 \leq x \leq 2\pi. f'(x) = 1 - \cos x \Rightarrow f''(x) = \sin x. \text{ Since } \sin x > 0 \text{ on } (0, \pi), f \text{ is concave upward on } (0, \pi).$