

$$10. y = \sin^{-1}(e^x) \Rightarrow y' = \frac{1}{\sqrt{1-(e^x)^2}} \cdot e^x = e^x / \sqrt{1-e^{2x}}$$

$$13. \frac{d}{dx}(xy^4 + x^2y) = \frac{d}{dx}(x + 3y) \Rightarrow x \cdot 4y^3y' + y^4 \cdot 1 + x^2 \cdot y' + y \cdot 2x = 1 + 3y' \Rightarrow$$

$$y'(4xy^3 + x^2 - 3) = 1 - y^4 - 2xy \Rightarrow y' = \frac{1 - y^4 - 2xy}{4xy^3 + x^2 - 3}$$

$$19. y = \log_5(1 + 2x) \Rightarrow y' = \frac{1}{(1 + 2x) \ln 5} \frac{d}{dx}(1 + 2x) = \frac{2}{(1 + 2x) \ln 5}$$

$$21. \sin(xy) = x^2 - y \Rightarrow \cos(xy)(xy' + y \cdot 1) = 2x - y' \Rightarrow x \cos(xy)y' + y' = 2x - y \cos(xy) \Rightarrow$$

$$y'[x \cos(xy) + 1] = 2x - y \cos(xy) \Rightarrow y' = \frac{2x - y \cos(xy)}{x \cos(xy) + 1}$$

$$26. y = \frac{(x^2 + 1)^4}{(2x + 1)^3(3x - 1)^5} \Rightarrow$$

$$\ln y = \ln \frac{(x^2 + 1)^4}{(2x + 1)^3(3x - 1)^5} = \ln(x^2 + 1)^4 - \ln[(2x + 1)^3(3x - 1)^5]$$

$$= 4 \ln(x^2 + 1) - [\ln(2x + 1)^3 + \ln(3x - 1)^5] = 4 \ln(x^2 + 1) - 3 \ln(2x + 1) - 5 \ln(3x - 1) \Rightarrow$$

$$\frac{y'}{y} = 4 \cdot \frac{1}{x^2 + 1} \cdot 2x - 3 \cdot \frac{1}{2x + 1} \cdot 2 - 5 \cdot \frac{1}{3x - 1} \cdot 3 \Rightarrow y' = \frac{(x^2 + 1)^4}{(2x + 1)^3(3x - 1)^5} \left(\frac{8x}{x^2 + 1} - \frac{6}{2x + 1} - \frac{15}{3x - 1} \right).$$

[The answer could be simplified to $y' = -\frac{(x^2 + 56x + 9)(x^2 + 1)^3}{(2x + 1)^4(3x - 1)^6}$, but this is unnecessary.]

$$27. y = x \tan^{-1}(4x) \Rightarrow y' = x \cdot \frac{1}{1 + (4x)^2} \cdot 4 + \tan^{-1}(4x) \cdot 1 = \frac{4x}{1 + 16x^2} + \tan^{-1}(4x)$$

$$42. x^2 + 4xy + y^2 = 13 \Rightarrow 2x + 4(xy' + y \cdot 1) + 2yy' = 0 \Rightarrow x + 2xy' + 2y + yy' = 0 \Rightarrow$$

$$2xy' + yy' = -x - 2y \Rightarrow y'(2x + y) = -x - 2y \Rightarrow y' = \frac{-x - 2y}{2x + y}.$$

At $(2, 1)$, $y' = \frac{-2 - 2}{4 + 1} = -\frac{4}{5}$, so an equation of the tangent line is $y - 1 = -\frac{4}{5}(x - 2)$, or $y = -\frac{4}{5}x + \frac{13}{5}$.

The slope of the normal line is $\frac{5}{4}$, so an equation of the normal line is $y - 1 = \frac{5}{4}(x - 2)$, or $y = \frac{5}{4}x - \frac{3}{2}$.

$$59. y = [\ln(x + 4)]^2 \Rightarrow y' = 2[\ln(x + 4)]^1 \cdot \frac{1}{x + 4} \cdot 1 = 2 \frac{\ln(x + 4)}{x + 4} \text{ and } y' = 0 \Leftrightarrow \ln(x + 4) = 0 \Leftrightarrow$$

$$x + 4 = e^0 \Rightarrow x + 4 = 1 \Leftrightarrow x = -3, \text{ so the tangent is horizontal at the point } (-3, 0).$$

$$61. x^2 + 2y^2 = 1 \Rightarrow 2x + 4yy' = 0 \Rightarrow y' = -x/(2y) = 1 \Leftrightarrow x = -2y. \text{ Since the points lie on the ellipse, we have}$$

$$(-2y)^2 + 2y^2 = 1 \Rightarrow 6y^2 = 1 \Rightarrow y = \pm \frac{1}{\sqrt{6}}. \text{ The points are } \left(-\frac{2}{\sqrt{6}}, \frac{1}{\sqrt{6}}\right) \text{ and } \left(\frac{2}{\sqrt{6}}, -\frac{1}{\sqrt{6}}\right).$$